## Neural networks Restricted Boltzmann machine - example



# RESTRICTED BOLTZMANN MACHINE

**Topics:** RBM, visible layer, hidden layer, energy function



Energy function: 
$$E(\mathbf{x}, \mathbf{h}) = -\mathbf{h}^{\top} \mathbf{W} \mathbf{x} - \mathbf{c}^{\top} \mathbf{x} - \mathbf{b}^{\top} \mathbf{h}$$
  
 $= -\sum_{j} \sum_{k} W_{j,k} h_{j} x_{k} - \sum_{k} c_{k} x_{k} -$ 

 partition function (intractable)

 $\sum_{i} b_{j}h_{j}$ 

## EXAMPLE OF DATA SET: MNIST

| 3 | 8 | 6 | 9 | 6 | 4 | 5 | З | 8 | Ц | ς          | 2  | 3 | 8 | 4 |  |
|---|---|---|---|---|---|---|---|---|---|------------|----|---|---|---|--|
| l | 5 | Ø | 5 | 9 | 7 | Ч |   | 6 | 3 | 0          | ٩  | 2 | б | 9 |  |
| 1 | 3 | 6 | 8 | 0 | う | 7 | 6 | 8 | ٩ | $\bigcirc$ | 3  | 8 | S | 2 |  |
| 8 | Ŷ | 4 |   | 3 | ٩ | K |   |   | 0 | 6          | Ş  | 5 | 0 |   |  |
| F | 2 | 7 | 3 | ١ | 4 | 0 | 5 | 0 | 6 | 8          | 7  | 6 | 8 | 9 |  |
| 4 | 0 | 6 | 1 | ٩ | 2 | L | 3 | 9 | Ц | 1          | كر | 6 | 6 | ) |  |
| L | З | 6 | 9 | 7 | 0 | 9 |   | 6 | 2 | જ          | 3  | 6 | 4 | 9 |  |
| 8 | 6 | z | 7 | B | S | 6 | 9 | 1 | 7 | 6          | 0  | 9 | 6 | 7 |  |



### FILTERS (LAROCHELLE ET AL., JMLR2009)

| 0     | 1    |    | 2  | •  |     | (C) |    | -   | •   | 10         |   | 1 | 0    | 1 |
|-------|------|----|----|----|-----|-----|----|-----|-----|------------|---|---|------|---|
| alle. | (10) | T. | 4  | 1  | C   |     | 1  |     | 6   | JA.        | E | N | 1    |   |
| Te :  | -    |    |    | •  | •   |     |    | (D) | i   | (*         | - | 0 | 10%  | Û |
| 1     | •    |    | 1ª | 2  | (   | 6   | (1 | 1.  | (3) | 2.         | 0 | 0 | 1    | 6 |
| 1     | 12   | 1  | •  | 60 | 3   | 2   | 3  | 9   | 4   | 3          | 2 | X | te.  | 1 |
| ik    | •    | 1  | *  | 0  | 11  | 14  |    | 2   | Ē   | The second | 9 | 1 | Ter. | 1 |
| (·    |      | 1  | •  | 0  | 1/2 | (   | 1  | -   |     | D          | • |   | 2    | 5 |
| 5     | ()   | ō  |    |    | -   | 0   | -  |     |     | ¢          |   |   | E.   |   |



## DEBUGGING

### **Topics:** stochastic reconstruction, filters

- Unfortunately, we can't debug with a comparison with finite difference
- We instead rely on approximate "tricks"
  - we plot the average stochastic reconstruction  $||\mathbf{x}^{(t)} \tilde{\mathbf{x}}||^2$  and see if it tends to decrease:
  - for inputs that correspond to image, we visualize the connection coming into each hidden unit as if it was an image
    - gives an idea of the type of visual feature each hidden unit detects
  - we can also try to approximate the partition function Z and see whether the (approximated) NLL decreases
    - On the Quantitative Analysis of Deep Belief Networks. Ruslan Salakhutdinov and Iain Murray, 2008